

# Representing n-ary Relations in DL

## A Generic Reification Strategy

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## Outline

Introduction

The Conventional Strategy

Best Practise Driven Reification

A Generic Reification Strategy

Conclusion

## The problem

Description logics are usually restricted to the two-variable fragment of first order logic:

### binary predicate

Natural language: Every book has an author.  
First order logic:  $\forall x(Bx \supset \exists y(Ryx \wedge Hy))$   
Description logic:  $B \sqcap \exists R.H$



### ternary predicate

Natural language: Every critic criticises somebody for something.  
First order logic:  $\forall x(Cx \supset \exists y \exists z(Sxyz \wedge Hy \wedge Tz))$   
Description logic: ?





## Ternary Relations in the Biomedical Domain

1. Cell  $C$  has organelle  $O$  with function  $F$ .
2. Disposition  $D$  has realisation  $R$  under conditions  $C$  (cf. Schulz/Jansen 2009).
3. Disorder  $D$  has morphology  $M$  at site  $S$  (cf. Spackman et al. 2002).

Irreducible ternary relations? Some tests:

1. Is the function predicated of the cell or the organelle? Clearly of the organelle.  
Two 'daisy-chained' binary relations:  $C$ has\_part $O$  and  $O$ has\_function $F$ .
2. Does the disposition have the conditions or does the realisation have them?  
Neither dispositions nor realisations simply have conditions. This is a true ternary relation.
3. Does the morphology have a site or does the site have the morphology?  
Arbitrary decisions. Cannot be analysed into 'daisy-chained' binary relations.



## Ternary Relations in the Biomedical Domain

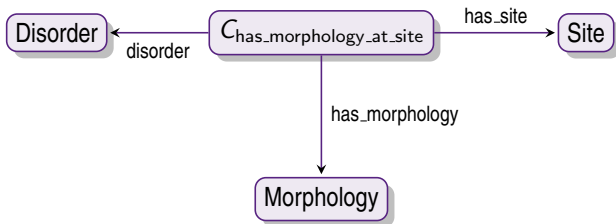
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## Reification

Representing relations as classes





## Problems

- Uniqueness constraints enforced by set-theoretical semantics don't apply. (When are two reified relations the same?)
- Role composition, transitive closure etc. are not possible for reified relations.
- Introduces classes for mere technical reasons, lacking clear ontological status.
- Causes a proliferation of classes and roles, impeding manageability of the ontology.
- Design of the reifications is at the modellers liberty. Quality varies.
- Different reification strategies can hinder ontology alignment.



## Reification Best Practises

Cf. Severi/Fiadeiro/Ekserdjian 2010

*[The] problem lies first of all in helping modellers to conceptualize the real world in a way that can lead to a better representation [...]. By 'better' we mean a more controlled use of reification and a closer fit between the resulting ontology and the real-world domain [...].*  
(Severi/Fiadeiro/Ekserdjian 2010, 417)

- Less is more: Try to use as few reified relations as possible.
- Be smart about it: Reify sub-relations that correspond to proper ontological classes.
- Reuse: Prefer to reify relations that partake in many other relations.





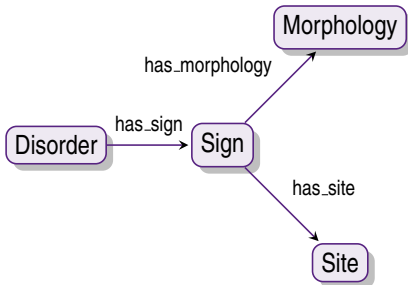
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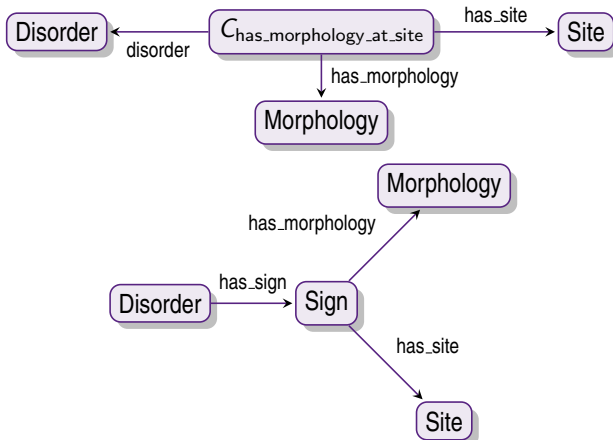
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## Smarter Reification







## Remaining Problems

- Does not ensure inter-modeller consistency.
- Requires ontologically 'fitting' classes to be identified.
- Necessary constraints need to be enforced on a case by case basis.

Desideratum: A 'fallback' strategy that

- can be used independently from domain ontology considerations
- minimizes inter-modeller variability
- makes modelling mistakes unlikely

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## Generic Reified Relations in DL

**Strategy:** Explicitly encode crucial features of relations in DL classes describing the arguments of a relation

- Order
- Arity
- Value ranges

### Order and value ranges

Using the primitive roles *has\_value* and *succeeds* to construct a class 'Argument':

$$\begin{aligned} \text{Argument} \equiv & \forall \text{succeeds}.\text{Argument} \sqcap \leq 1 \text{succeeds} \sqcap \\ & \leq 1 \text{succeeds}^- \sqcap = 1 \text{has\_value}.\top \\ \text{Dis}(\text{succeeds}, & \text{succeeds}^-) \end{aligned}$$



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## Generic Reified Relations in DL

continued...

### Arity 1

It is tempting to define the class 'Relation' with a *has\_argument* role and a role composition axiom:

$$\text{Relation} \equiv \geq 1 \text{ has\_argument}.\text{Argument}$$

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*SROIQ* (and hence OWL 2) only allows simple roles in number restrictions!





## Generic Reified Relations in DL

Arity II

**Workaround:** Explicitly model beginning and end of the argument chain.

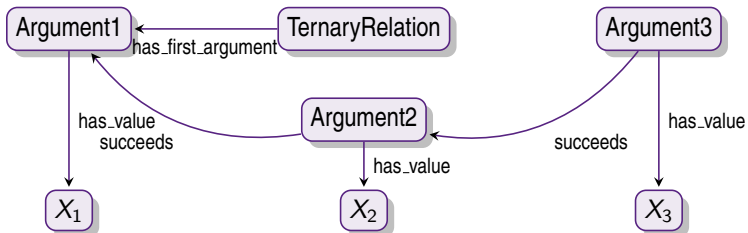
$$\text{Argument}_1 \equiv \text{Argument} \sqcap \neg \exists \text{succceeds} . \text{Argument} \sqcap \\ = 1 \text{ has\_first\_argument}^- . \text{Relation}$$

$$\text{Argument}_N \equiv \text{Argument} \sqcap \geq 1 \text{ succceeds} \sqcap \geq 1 \text{ succceeds}^-$$

$$\text{Argument}_{\text{Last}} \equiv \text{Argument} \sqcap \neg \exists \text{succceeds}^- . \text{Argument}$$

$$\text{Argument}_0 \sqcap \text{Argument}_N \equiv \perp$$

## Example: Ternary Relation



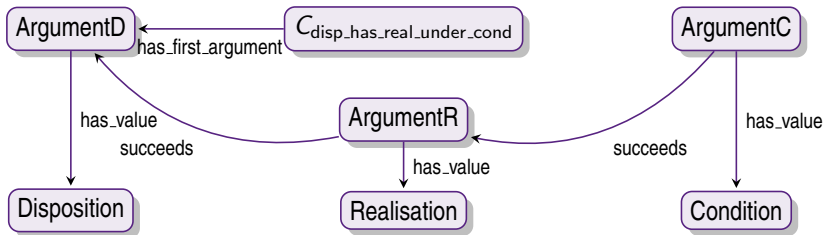
## How to use this framework

- The proposed generic structure of relations can be regarded as a template.
- For concrete relations that shall be reified, the structure is subclassed by simple value restrictions.

Analysing the disposition example:

$$\text{ArgumentD} \equiv \text{Argument1} \sqcap \forall \text{has\_value. Disposition}$$
$$\text{ArgumentR} \equiv \text{ArgumentN} \sqcap \exists \text{succeeds. ArgumentD} \sqcap \forall \text{has\_value. Realisation}$$
$$\text{ArgumentC} \equiv \text{ArgumentN} \sqcap \text{ArgumentLast} \sqcap$$
$$\exists \text{succeeds. ArgumentR} \sqcap \forall \text{has\_value. Condition}$$
$$C_{\text{disp\_has\_real\_under\_cond}} \equiv \text{Relation} \sqcap \exists \text{has\_first\_argument. ArgumentC}$$

## How to use this framework



## Performance

Performance measurements using the HerMiT reasoner:

	Ontology	Classification Time
BL	Baseline profile, 'toy'-ontology based on OGMS	13.69s
NA-20	BL + 20 reified ternary relations using the 'naïve' pattern	26,59s
R3-10	BL + 10 reified ternary relations using the new scheme	38,39s
R3-20	BL + 10 reified ternary relations using the new scheme	74,37s
R4-10	BL + 10 reified quaternary relations using the new scheme	73,67s



## Conclusion

### Benefits:

- Systematic framework for reified relations in the general case
- Does not 'pollute' the domain specific namespace
- Leaves little space for arbitrary modeller decisions
- Eases comparability and consistency

### Costs:

- Even greater proliferation of classes
- Notable performance penalty

### Open Questions:

- Where exactly can reified relations fit into a top-level ontology?
- Is it possible to hide the complexity resulting from the reification scheme?

Get the code:

<https://code.google.com/p/nrel-ontology-template/>



# Thank you!

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Good Ontology Design